# CS:5810 Formal Methods in Software Engineering

### Reasoning about Programs with Objects in Dafny

Copyright 2020-21, Graeme Smith and Cesare Tinelli.

Produced by Cesare Tinelli at the University of Iowa from notes originally developed by Graeme Smith at the University of Queensland. These notes are copyrighted materials and may not be used in other course settings outside of the University of Iowa in their current form or modified form without the express written permission of one of the copyright holders. During this course, students are prohibited from selling notes to or being paid for taking notes by any person or commercial firm without the express written permission of one of the copyress written permission of one of the copyress written permission of one of the copyress written permission of one of the copyright holders.

# **Checksum Objects**

An *object* is an instance of a *class*, and like arrays, has a *reference type* 

```
class ChecksumMachine {
                                     string is shorthand
  var data: string +
                                     for seq<char>
  constructor ()
    ensures data ==
                     method Append(d: string)
    modifies this
    ensures data == old(data) + d
  function method Checksum(): int
    reads this
    ensures Checksum() == Hash(data)
```

# **Checksum Objects**

```
...
function method Hash(s: string): int {
  SumChars(s) % 137
}
function method SumChars(s: string): int {
  if s == 0 then 0 else
   var last := |s| - 1;
    SumChars(s[..last]) + s[last] as int
}
                                converts char to int
```

# Test client

```
method Main() {
    var m := new ChecksumMachine();
    m.Append("green ");
    m.Append("grass");
    var c := m.Checksum();
    print "Checksum is ", c, "\n";
}
```

A method is allowed to allocate new arrays and objects and change their state (that is, the elements of the arrays and the fields of the objects) without mentioning these arrays and objects in the modifies clause

### **Class Invariant**

To write efficient implementation, want to keep track of checksum so far:

```
var cs: int
```

We want to use data in specifications, but not in compiled program:

```
ghost var data: string
predicate Valid() A predicate is a
   reads this Boolean function
{ cs == Hash(data) }
```

If a function accesses the fields of an object o, its specification must include reads o

### **Class Invariant**

```
class ChecksumMachine {
 ghost var data: string
  predicate Valid()
    reads this
  constructor ()
    ensures Valid() && data == ""
  method Append(d: string)
    requires Valid()
    modifies this
    ensures Valid() && data == old(data) + d
  function method Checksum(): int
    requires Valid()
    reads this
    ensures Checksum() == Hash(data)
}
```

# Implementation

```
constructor ()
    ensures Valid() && data == ""
{ cs := 0;
    data := ""
}
```

A constructor is allowed to assign to the fields of the object being constructed, this, without mentioning this in the modifies clause

```
function method Checksum(): int
  requires Valid()
  reads this
  ensures CheckSum() == Hash(data)
  { cs }
```

### Implementation

```
method Append(d: string)
  requires Valid()
 modifies this
  ensures Valid()
  ensures data == old(data) + d
  var i := 0;
  while i != |d|
    invariant 0 <= i <= |d|</pre>
    invariant Valid()
    invariant data == old(data) + d[..i]
  {
    cs := (cs + d[i] as int) % 137;
    data := data + [d[i]];
    i := i + 1;
```

# Coffee maker components

```
class Grinder {
                                   class WaterTank {
                                                                class Cup {
var HasBeans: bool
                                     var Level: nat
                                                                   constructor ()
                                   predicate Valid()
predicate Valid()
  reads this
                                     reads this
constructor ()
                                   constructor ()
                                      ensures Valid()
  ensures Valid()
method AddBeans()
                                   method Fill()
  requires Valid()
                                      requires Valid()
  modifies this
                                     modifies this
  ensures Valid() && HasBeans
                                      ensures Valid() && Level == 10
method Grind()
                                   method Use()
  requires Valid() && HasBeans
                                     requires Valid() && Level != 0
  modifies this
                                     modifies this
  ensures Valid()
                                      ensures Valid() && Level == old(Level) - 1
                                    }
```

# Coffee maker version 0

```
class CoffeeMaker {
  predicate Valid() reads this
  constructor () ensures Valid()
  predicate method Ready()
    requires Valid()
    reads this
  method Restock()
    requires Valid()
    modifies this
    ensures Valid() && Ready()
  method Dispense(double: bool) returns (c: Cup)
    requires Valid() && Ready()
    modifies this
    ensures Valid()
}
```

# Coffee maker version 0

#### State:

#### **Require:**

```
predicate Valid()
  reads this, g, w
```

Similar change also needed for reads of Ready() and modifies clauses of Restock and Dispense

#### **Representation sets**

The expanded modifies and reads clauses violate the principles of information hiding.

Therefore, we abstract the state of an object to a *representation set*.

For this implementation of the coffee maker, the representation set is

{o, o.g, o.w}

but the coffee maker may also be implemented in terms of different objects.

# Coffee maker version 1

Add new variable to state: ghost var Repr: set<object>

Change modifies clauses of Restock and Dispense to modifies Repr

Change read clauses of Valid and Ready to reads Repr

Add the following to the body of Valid this in Repr && g in Repr && g.Valid() && w in Repr && w.Valid()

Typically specify lower bound on objects in Repr

# Coffee maker version 1

In Valid:

reads Repr // error: insufficient reads clause

This is because this is not in Repr unless Valid's predicate holds (and Valid may return true or false).

```
We require:
    predicate Valid()
        reads this, Repr
    {
        this in Repr &&
        g in Repr && g.Valid() &&
        w in Repr && w.Valid()
    }
```

# **Class implementation**

```
constructor ()
  ensures Valid()
{
  g := new Grinder();
  w := new WaterTank();
  Repr := {this, g, w};
predicate method Ready()
  requires Valid()
  reads Repr
  g.HasBeans && 2 <= w.Level
```

# **Class implementation**

```
method Restock()
  requires Valid()
  modifies Repr
  ensures Valid() && Ready()
  g.AddBeans(); w.Fill();
method Dispense(double: bool) returns (c: Cup)
  requires Valid() && Ready()
  modifies Repr
   ensures Valid()
{
  g.Grind();
  if double { w.Use(); w.Use(); } else { w.Use(); }
  c := new Cup();
}
```

# Test harness

```
method CoffeeTestHarness() {
    var cm := new CoffeeMaker();
    cm.Restock(); // modifies clause violated
    var c := cm.Dispense(true); // modifies clause violated
}
```

The test harness has no modifies clause and so is only allowed to modify the fields of fresh objects

Our specification of the coffee maker didn't specify that created objects were fresh

# Coffee maker version 2

Add to constructor: ensures fresh(Repr)

This removes error with Restock, but not Dispense.

```
Add to Restock and Dispense:
ensures Repr == old(Repr)
```

Alternatively, make Repr immutable by declaring it as
 ghost const Repr: set<object>

# Changing Repr

What if implementation needs to change Repr, e.g., a method of the coffee maker needs to change the grinder?

Third (and preferred) alternative for ensures clauses of methods which mutate Repr:

ensures fresh(Repr - old(Repr))

That is, any new objects added to Repr are *fresh* 

#### Less common situations

```
method ChangeGrinder()
    requires Valid()
    modifies Repr
    ensures Valid() && fresh(Repr - old(Repr))
{
    g := new Grinder();
    Repr := Repr + {g};
}
```

Old grinder is still in Repr, but is no longer referenced

The run-time system will eventually reclaim the storage for this object

#### Less common situations

```
method InstallCustomGrinder(grinder: Grinder)
  requires Valid() && grinder.Valid()
  modifies Repr
  ensures Valid()
  ensures fresh(Repr - old(Repr) - {grinder})
  {
    g := grinder;
    Repr := Repr + {g};
}
```

### Less common situations

```
method InstallCustomGrinder(grinder: Grinder)
  requires Valid() && grinder.Valid()
  modifies Repr
  ensures Valid() && fresh(Repr - old(Repr) - {grinder})
  {
    g := grinder;
    Repr := Repr + {g};
  }
}
```

Since Repr can dynamically change, this approach to specification is referred to as *dynamic frames* 

Dafny is a permutation of certain letters in Dyn<sup>amic</sup> f<sup>r</sup>a<sup>mes</sup>

# Grinder as an aggregate

```
class Grinder {
   var HasBeans: bool
   ghost var Repr: set<object>
   predicate Valid()
      reads this, Repr
   constructor ()
      ensures Valid() && fresh(Repr)
   method AddBeans()
      requires Valid()
      modifies Repr
      ensures Valid() && HasBeans && fresh(Repr - old(Repr))
   method Grind()
      requires Valid() && HasBeans
      modifies Repr
      ensures Valid() && fresh(Repr - old(Repr))
   }
```

### WaterTank as an aggregate

```
class WaterTank {
  var Level: nat
   ghost var Repr: set<object>
   predicate Valid() reads this, Repr
   constructor () ensures Valid() && fresh(Repr)
   method Fill()
      requires Valid()
      modifies Repr
      ensures Valid() && fresh(Repr - old(Repr)) && Level == 10
  method Use()
      requires Valid() && Level != 0
      modifies Repr
      ensures Valid() && fresh(Repr - old(Repr))
                      && Level == old(Level) - 1
}
```

# **Coffee Maker**

#### Invariant (in Valid):

```
this in Repr &&
g in Repr && g.Repr <= Repr && g.Valid() &&
w in Repr && w.Repr <= Repr && w.Valid()</pre>
```

#### Constructor:

```
constructor ()
    ensures Valid() && fresh(Repr)
{
    g := new Grinder();
    w := new WaterTank();
    Repr := {this, g, w} + g.Repr + w.Repr;
} // illegal first-phase use of fields
```

# Constructor

First phase set objects fields and define immutable values

- objects are still being constructed
- so, this.g.Repr is not allowed for example

```
Avoid use of uninitialized fields:
    var gg := new Grinder();
    var ww := new WaterTank();
    g, W := gg, WW;
    Repr := {this, g, w} + gg.Repr + ww.Repr;
```

Update Repr in second phase:

```
g := new Grinder(); w := new WaterTank();
new;
Repr := {this, g, w} + g.Repr + w.Repr;
```

```
method Restock()
    requires Valid()
    modifies Repr
    ensures Valid() && fresh(Repr - old(Repr)) && Ready()
{
```

g.AddBeans();

w.Fill(); // precondition violation; modifies violation
} // postcondition violation

```
method Restock()
    requires Valid()
    modifies Repr
    ensures Valid() && fresh(Repr - old(Repr)) && Ready()
{
```

```
g.AddBeans();
assert w.Valid(); // assertion violation
w.Fill(); // modifies violation
} // postcondition violation
} // postcondition violation
} // postcondition violation
```

```
method Restock()
  requires Valid()
  modifies Repr
  ensures Valid() && fresh(Repr - old(Repr)) && Ready()
  assert w.Valid();
                                              Call to AddBeans
                                              affects w.Valid()
  g.AddBeans();
  assert w.Valid(); // assertion violation
  w.Fill(); // modifies violation
} // postcondition violation
```

```
method Restock()
  requires Valid()
  modifies Repr
  ensures Valid() && fresh(Repr - old(Repr)) && Ready()
{
  assert w.Valid();
                                              Call to AddBeans
                                              affects w.Valid()
  g.AddBeans();
  assert w.Valid(); // assertion violation
  w.Fill(); // modifies violation
} // postcondition violation
```

g.AddBeans only modifies g.Repr, and w.Valid only reads w.Repr This suggests there is an overlap between g.Repr and w.Repr

```
method Restock()
  requires Valid()
  modifies Repr
  ensures Valid() && fresh(Repr - old(Repr)) && Ready()
{
  assert w.Valid();
  assert g.Repr !! w.Repr; // assertion violation
  g.AddBeans();
  assert w.Valid(); // assertion violation
  w.Fill(); // modifies violation
} // postcondition violation
```

(A !! B) states that sets A and B are disjoint (A \* B == {})

```
method Restock()
  requires Valid()
  modifies Repr
  ensures Valid() && fresh(Repr - old(Repr)) && Ready()
{
  assert this !in g.Repr; // assertion violation
  assert g in g.Repr; // assertion violation
  assert w !in g.Repr; // assertion violation
  assert w.Valid();
  assert g.Repr !! w.Repr; // assertion violation
  g.AddBeans();
  assert w.Valid(); // assertion violation
  w.Fill(); // modifies violation
} // postcondition violation
```

# Coffee Maker invariant

#### Valid:

```
this in Repr && g in Repr &&
g.Repr <= Repr &&
this !in g.Repr && g.Valid() &&
w in Repr && w.Repr <= Repr &&
this !in w.Repr && w.Valid() &&
g.Repr !! w.Repr</pre>
```

If body of Valid() is hidden from clients then they can't see this in Repr. Hence, update postcondition of *all* validity predicates as follows

```
predicate Valid()
    reads this, Repr
    ensures Valid() ==> this in Repr
```

### Back to Restock

```
method Restock()
    requires Valid()
    modifies Repr
    ensures Valid() && fresh(Repr - old(Repr)) && Ready()
{
    g.AddBeans();
    w.Fill();
```

} // postcondition violation

Calls to AddBeans and Fill may expand g.Repr and w.Repr

### **Back to Restock**

```
method Restock()
    requires Valid()
    modifies Repr
    ensures Valid() && fresh(Repr - old(Repr)) && Ready()
{
      g.AddBeans();
      w.Fill();
      Repr := Repr + g.Repr + w.Repr;
} // postcondition violation
```

### **Back to Restock**

```
method Restock()
    requires Valid()
    modifies Repr
    ensures Valid() && fresh(Repr - old(Repr)) && Ready()
{
      g.AddBeans();
      w.Fill();
      Repr := Repr + g.Repr + w.Repr;
} // postcondition violation
```

What we did on the relationships between frames holds for Dispense too. We just need to add the following to its body:

```
Repr := Repr + g.Repr + w.Repr;
```

# Summary

#### **Representation set:**

```
ghost var Repr: set<object>
```

#### Invariant:

```
predicate Valid()
  reads this, Repr
  ensures Valid() ==> this in Repr
  { this in Repr && ... }
  a in Repr && a.Valid()
  b in Repr && b.Repr <= Repr &&
  this !in b.Repr && b.Valid()
  a0 != a1 &&
  {a0, a1} !! b0.Repr !! b1.Repr
```

a, a0, a1 are objects with simple frames

b, b0, b1 are objects with dynamic frames

# Summary

```
Constructor:
  constructor ()
     ensures Valid() && fresh(Repr)
  { ...; Repr := {this, a, b} + b.Repr; }
Functions:
  function F(x: X): Y
     requires Valid()
     reads Repr
(Mutating) method:
  method M(x: X) returns (y: Y)
     requires Valid()
     modifies Repr
     ensures Valid() && fresh(Repr - old(Repr))
```