CS:5810 Formal Methods in Software Engineering

Reasoning About Programs in Dafny

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Program Correctness

Is this program fragment correct?

Recall: A program can only be said to be correct with respect to a specification

Correctness

Is this program fragment correct with respect to the following specification?

"Given integers a and b, the program produces in x the product of a and b"

Correctness

Is this program fragment correct with respect to the following specification?

"Given **positive** integers a and b, the program produces in x the product of a and b"

Design by Contract

Specification of example program:

"Given positive integers a and b, the program produces in x the product of a and b"

> requires a and b to be positive integers ensures x is the product of a and b

Precondition: caller needs to ensure this to get a meaningful result

Postcondition: callee guarantees this when precondition is met

Timsort

- Timsort is a sorting algorithm developed for Python by Tim Peters in 2002.
- It uses a combination of merge sort and insertion sort.
- It was designed to perform well on real-world data (with *runs* of descending values, and of non-descending values).
- Ported to Java 1.7 (java.util.Collections.sort and java.util.Arrays.sort) in 2011.
- Default sorting algorithm for Android SDK, Oracle's JDK and Open JDK.

Timsort bug

Bug in Timsort discovered in 2015.

git clone https://github.com/abstools/java-timsort-bug.git
cd java-timsort-bug
javac *.java
java TestTimSort 67108864

leads to

```
Exception in thread "main"
java.lang.ArrayIndexOutOfBoundsException: 40
at java.util.TimSort.pushRun(TimSort.java:413)
at java.util.TimSort.sort(TimSort.java:240)
at java.util.Arrays.sort(Arrays.java:1438)
at TestTimSort.main(TestTimSort.java:18)
```



Stijn de Gouw CWI, The Netherlands

Formal verification

To formally verify a program you need

- A formal (i.e., mathematical) specification
- A formal proof
- Automated tools (Timsort found using the KeY tool)
- Expertise

Learning about specification and proof sharpens thinking

Formal verification

Some program verification tools

- KeY, OpenJML Java
- VCC, Verifast, Smack C
- Spec# C#
- Stainless, Sireum Scala
- Why3 WhyML
- Dafny

– Dafny

Formal verification



Educational objectives

Learn how to

- specify precisely what a program is supposed to do
- verify that a program behaves as specified
- derive a program that behaves as specified
- use the Dafny programming language and verifier for that

```
method Triple(x: int) returns (r: int)
    ensures r == 3 * x
{
    var y := 2 * x;
    r := x + y;
}
```

The caller should not be able to see a method's body, only its specification

The specification describes the method's behavior, abstracting from the details of the method's body

```
method Triple(x: int) returns (r: int)
  ensures r == 3 * x
{
  var y := Double(x);
  r := x + y;
}
```

```
method Double(x: int) returns (r: int)
  ensures r == 2 * x
```

```
method Triple(x: int) returns (r: int)
  requires x >= 0
  ensures r == 3 * x
{
    var y := Double(x);
    r := x + y;
}
```

method Double(x: int) returns (r: int)
 requires x >= 0
 ensures r == 2 * x

```
method Triple(x: int) returns (r: int)
  ensures r == 3 * x
{
  if x >= 0 {
   var y := Double(x); r := x + y;
  } else {
   var y := Double(-x); r := x - y;
  }
}
method Double(x: int) returns (r: int)
```

```
method Double(x: int) returns (r: int)
  requires x >= 0
  ensures r == 2 * x
```

Logic in Dafny

true false	
! A	"not A"
A && B	"A and B"
A B	"A or B"
A ==> B	"A implies B" or "A only if B"
A <==> B	"A if and only if B"
Precedence order: ! &&	==> <==>
forall x :: A	"for all x, A is true"
exists x :: A	"there exists an x such that A is true"

Program state

```
method MyMethod(x: int) returns (y: int)
  requires x >= 10
  ensures y >= 25
{
    var a := x + 3;
    var b := 12;
    y := a + b;
}
```

The program variables x, y, a, and b, collectively constitute the method's *state*

Note: not all program variables are in scope the whole time

```
method MyMethod(x: int) returns (y: int)
  requires x >= 10
  ensures y >= 25
{
  // here, we know x \ge 10
  var a := x + 3;
  // here, a == x+3 && x >= 10
  var b := 12;
  // here, a == x+3 && x >= 10 && b == 12
  y := a + b;
 // here, a == x+3 && x >= 10 && b == 12 &&
  // y == a + b
}
```



```
method MyMethod(x: int) returns (y: int)
 requires x >= 10
  ensures y >= 25
{
 // here, we want x + 3 + 12 >= 25
 var a := x + 3;
 // here, we want a + 12 >= 25
 var b := 12;
 // here, we want a + b \ge 25
  y := a + b;
 // here, we want y \ge 25
}
```

```
method MyMethod(x: int) returns (y: int)
  requires x >= 10
  ensures y >= 25
  // here, we want x + 3 + 12 >= 25
                                         Last calculated
  var a := x + 3;
  // here, we want a + 12 >= 25
                                         condition is implied
                                         by the stated
  var b := 12;
                                         precondition
  // here, we want a + b >= 25
  y := a + b;
  // here, we want y \ge 25
```

Exercise 1

Consider a method with the type signature below which returns in s to the sum of x and y and in m the maximum of x and y:

method MaxSum(x: int, y: int) returns (s: int, m: int)

Write the postcondition specification for this method

Exercise 2

Consider a method that attempts to reconstruct the arguments x and y from the return values of MaxSum in Exercise 1. In other words, consider a method with the following type signature and same postcondition as the method of Exercise 1:

method ReconstructFromMaxSum(s: int, m: int)
returns (x: int, y: int)

This method cannot be implemented. Write an appropriate precondition for the method that allows you to implement it.