CS:5810 Formal Methods in Software Engineering

Case Study: Hotel Lock System

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Acknowledgments

These notes are based on an Alloy example in the book:

[Jack06] Daniel Jackson. Software abstractions – Logic, Language, and Analysis. The MIT press, 2006.

The Task

- Model in Alloy the disposable card key system used in most hotels for locking and unlocking guest rooms
- The system uses recordable locks, which prevent previous guests from entering a room once its has been re-assigned
- We will model both static and dynamic aspects of the system

Problem Description [Jack06]

"[...] the hotel issues a new key to the next occupant, which recodes the lock, so that previous keys will no longer work.

The lock is a simple, stand-alone unit [...] with a memory holding the current key combination.

A hardware device [...] [within the lock] generates a sequence of pseudorandom numbers."

Problem Description [Jack06]

"The lock is opened either by the current key combination, or by its successor;

If a key with the successor is inserted, the successor is made to be the current combination, so that the old combination will no longer be accepted.

This scheme requires no communication between the front desk and the door lock."

Problem Description [Jack06]

"By synchronizing the front desk and the door locks initially, and by using the same pseudorandom generator,

the front desk can keep its records of the current combinations in step with the doors themselves."

Signatures: Key, Room, Guest, FrontDesk

- Key refers to the key combination stored in the magnetic strip of the card
- FrontDesk stores at any time a mapping
 - between each room and its most recent key combination (if any), and
 - between each room and its current guest

- Room refers to the room lock
- Each room (lock) has
 - an associated set of possible keys, and
 - exactly one current key at a time
- Each key belongs to at most one room
- Each guest has zero or more keys at any time

```
module hotel
open util/ordering [Key] as KO
```

}

```
module hotel
open util/ordering [Key] as KO
sig Key {}
sig Room {
  keys: set Key,
  var currentKey: Key
sig Guest {
  var keys: set Key
one sig FrontDesk {
  var lastKey: Room -> lone Key,
  var occupant: Room -> Guest
```

Room Constraint

Each key belongs to at most one room

```
fact {
   all k: Key | lone keys.k
}
```

New Key Generation

Given a key k and a set ks of keys, nextKey returns the smallest key (in the key ordering) in ks that follows k

```
fun nextKey [k: Key, ks: set Key]: set Key
{
   KO/min [KO/nexts[k] & ks]
}
```

Initial State

```
module examples/hotel
open util/ordering [Key] as KO
sig Key {}
sig Room {
  keys: set Key,
                                      No constraints
  var currentKey: Key
                                           the record of each room's key at
                                           the front desk is synchronized
sig Guest {
  var keys: set Key  No guests have keys
                                           with the current combination of
                                           the lock itself
one sig FrontDesk {
 var lastKey: Room -> lone Key,
 var occupant: Room -> Guest
                                          No rooms are occupied
```

Hotel Operations: Initial State

```
pred init [] {
  -- no guests have keys
  no Guest.keys
  -- the roster at the front desk shows
  -- no room as occupied
  no FrontDesk.occupant
  -- the record of each room's key at the
  -- front desk is synchronized with the
  -- current combination of the lock itself
  all r: Room
   r.(FrontDesk.lastKey) = r.currentKey
```

Hotel Operations: Guest Entry

```
pred entry [ g: Guest, r: Room, k: Key ]
```

- Preconditions:
 - The key used to open the lock is one of the keys the guest is holding
- Pre and Post Conditions:
 - The key on the card
 - either matches the lock's current key, and the lock remains unchanged (not a new guest), or
 - matches its successor, and the lock is advanced (new guest)
- Frame conditions:
 - no changes to the state of other rooms, or to the set of keys held by guests, or to the records at the front desk

Hotel Operations: Guest Entry

```
pred entry[ g:Guest, r:Room, k:Key ] {
  -- the key used to open the lock is one of
  -- the keys the guest is holding
  k in g.keys
  -- pre and post conditions
  let ck = r.currentKey |
    -- not a new guest
    (k = ck \text{ and } ck' = ck) \text{ or }
    -- new guest
     (k = nextKey[ck, r.keys] and ck' = k)
  -- frame conditions
  noFrontDeskChange
  noRoomChangeExcept[r]
  noGuestChangeExcept[none]
```

Frame Condition Predicates

```
pred noFrontDeskChange []
  FrontDesk.lastKey' = FrontDesk.lastKey
  FrontDesk.occupant' = FrontDesk.occupant
pred noRoomChangeExcept [rs: set Room]
  all r: Room - rs |
    r.currentKey' = r.currentKey
pred noGuestChangeExcept [gs: set Guest]
  all g: Guest - gs | g.keys' = g.keys
```

Hotel Operations: Check-out

```
pred checkout [ g: Guest ]
```

- Preconditions:
 - the guest occupies one or more rooms
- Postconditions:
 - the guest's rooms become available
- Frame conditions:
 - Nothing changes but the occupant relation

Hotel Operations: Check-out

```
one sig FrontDesk {
    lastKey: Room -> lone Key,
    occupant: Room -> Guest
pred checkout [ g: Guest ]
    let occ = FrontDesk.occupant | {
      -- the guest occupies one or more rooms
      some occ.q
      -- the guest's rooms become available
      occ.' = occ - (Room -> q)
    -- frame condition
    FrontDesk.lastKey' = FrontDesk.lastKey
    noRoomChangeExcept[none]
    noGuestChangeExcept[none]
```

Hotel Operations: Check-in

```
pred checkin [ g: Guest, r: Room, k: Key ]
```

- Preconditions:
 - the room is available
 - the input key is the successor of the last key in the sequence associated to the room
- Postconditions:
 - the guest holds the input key and becomes the new occupant of the room
 - the input key becomes the room's current key
- Frame conditions:
 - Nothing changes but the occupant relation and the guest's relations

Hotel Operations: Check-in

```
pred checkin [ g: Guest, r: Room, k: Key ] {
  let occ = FrontDesk.occupant |
  let lk = FrontDesk.lastKey | {
     -- the room has no current occupant
     no r.occ
     -- the input key is the successor of the last key in
     -- the sequence associated to the room
     k = nextKey[r.]k, r.keys]
     -- the guest becomes the new occupant of the room
     occ.t = occ + (r -> g)
     -- the guest holds the input key
     g.keys' = g.keys + k
     -- the input key becomes the room's current key
     1k' = 1k ++ (r -> k)
  noRoomChangeExcept
  noGuestChangeExcept[g]
```

Trace Generation

- The first time step satisfies the initialization conditions
- Any pair of consecutive time steps are related by
 - an entry operation, or
 - a check-in operation, or
 - a check-out operation

Trace Generation

```
fact Traces {
  init
  always
    some g: Guest, r: Room, k: Key
      entry[g, r, k] or
      checkin[g, r, k] or
      checkout[g]
```

Analysis

- Let's check if unauthorized entries are possible:
 - If a guest g enters room r at time t, and the front desk records show r as occupied at that time, then g must be a recorded occupant of r.

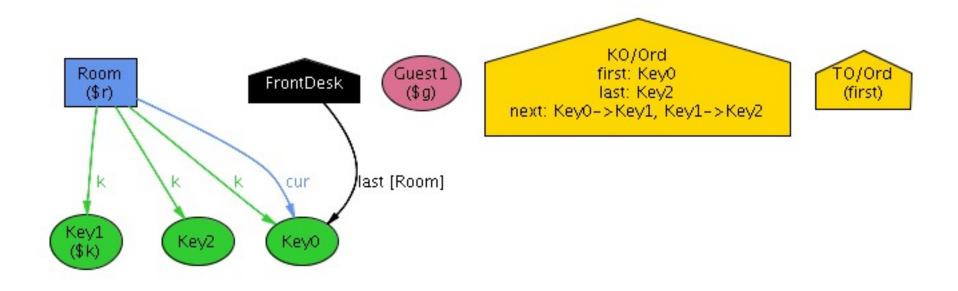
```
assert noBadEntry {
   always all r: Room, g: Guest, k: Key |
    let o = r.FrontDesk.occupant |
        (entry[g, r, k] and some o) implies g in o
}
```

Analysis

```
check noBadEntry for 3
but 2 Room, 2 Guest, 5 Time
```

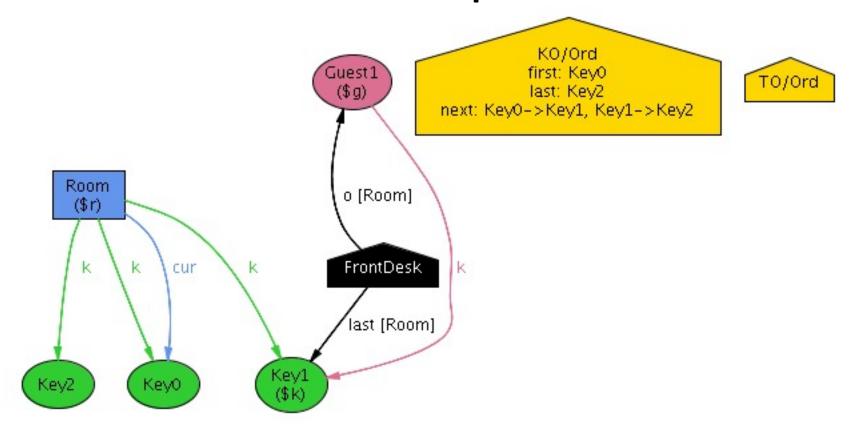
- It is enough to check for problem already with just 2 guests and 2 rooms
- Time's scope must be at least 5 because at least 4 time steps are needed to execute each operation once.
- There is a counter-example
 (see file dynamic/hotel1-elec.als)

TO: Initial State



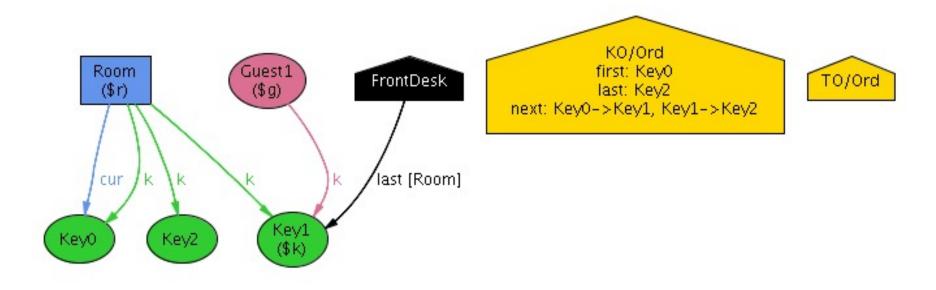
Initially, the current key of Room is KeyO, which is also reflected in the front desk's record

T1: Checkin Operation



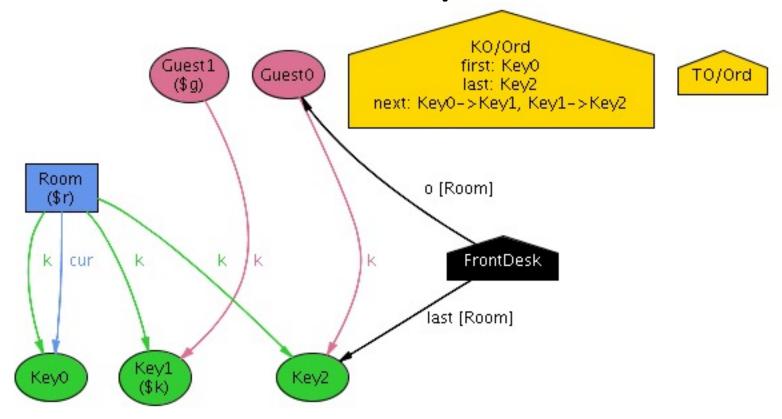
Guest1 checks in to Room and receives key Key1; the occupancy roster at the front desk is updated accordingly; Key1 is recorded as the last key assigned to Room

T2: Checkout Operation



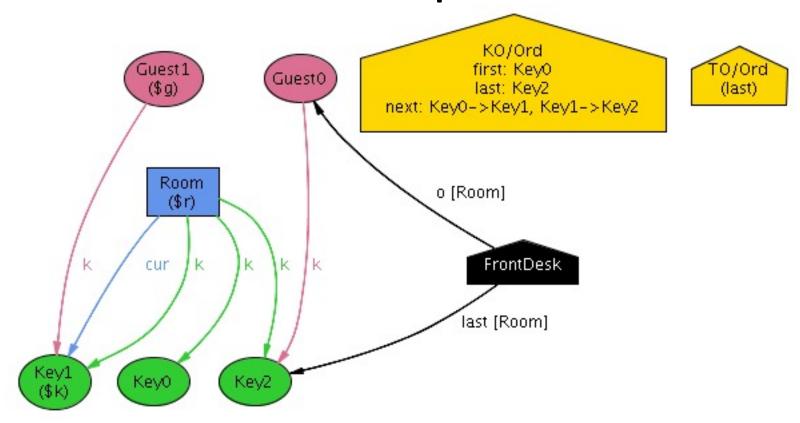
Guest1 checks out, and the occupancy roster is cleared

T3: Checkin Operation



Guest0 checks in to Room and receives key Key2; the occupancy roster at the front desk is updated accordingly; Key2 is recorder as the last key assigned to Room

T4: Enter Operation



Guest1 presents Key1 to the lock of Room, and is admitted

Necessary Restriction

There must be no intervening operation between a guest's check-in and room entry

```
pred noIntervening [] {
   always
   all g: Guest, r: Room, k: Key |
      checkin[g, r, k] implies
      after entry[g, r, k]
}
```

Conditional Assertion

Make assertion under noIntervening assumption

```
assert noBadEntry {
  noIntervening =>
  always all r: Room, g: Guest, k: Key |
   let o = r.FrontDesk.occupant |
      (entry[g, r, k] and some o) implies
      g in o
}
```

Analysis

We check once again:

```
check noBadEntry for 3
but 2 Room, 2 Guest, 5 Time
```

- No counter-example (see file dynamic/hotel2-elec.als)
- For greater confidence, we increase the scope:

```
check noBadEntry for 5
but 3 Room, 3 Guest, 20 Time
```

No counter-examples