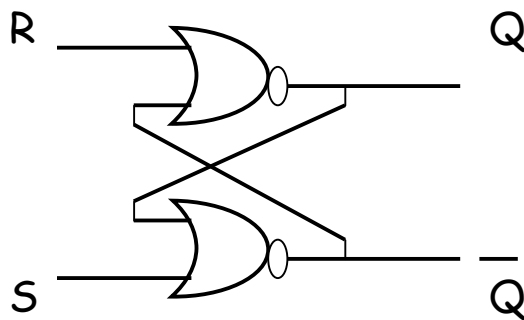


# Sequential Circuits

The output depends not only on the current inputs, but also on the past values of the inputs. This is how a digital circuit remembers data. Let us see how a single bit is stored.

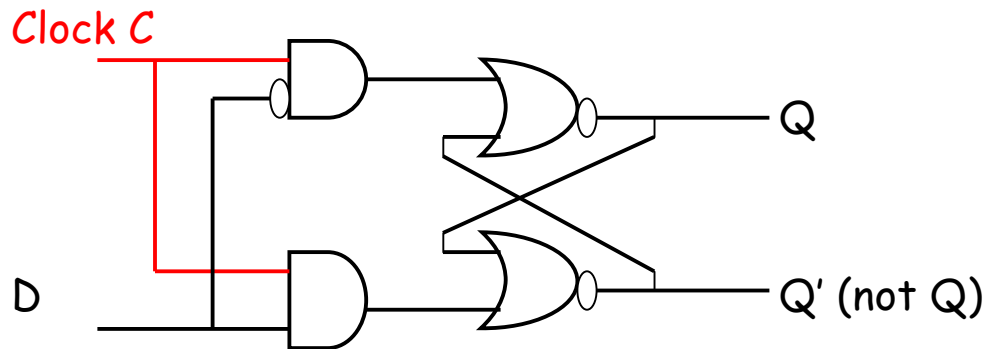


An SR Latch

R = Reset, S = Set

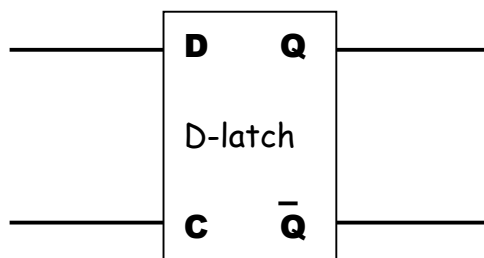
S	R	Q	$\bar{Q}$	Comment
0	0	0/1	1/0	Old state continues
1	0	1	0	Set state
0	1	0	1	Reset state
1	1	0	0	Illegal inputs

## A clocked D-latch



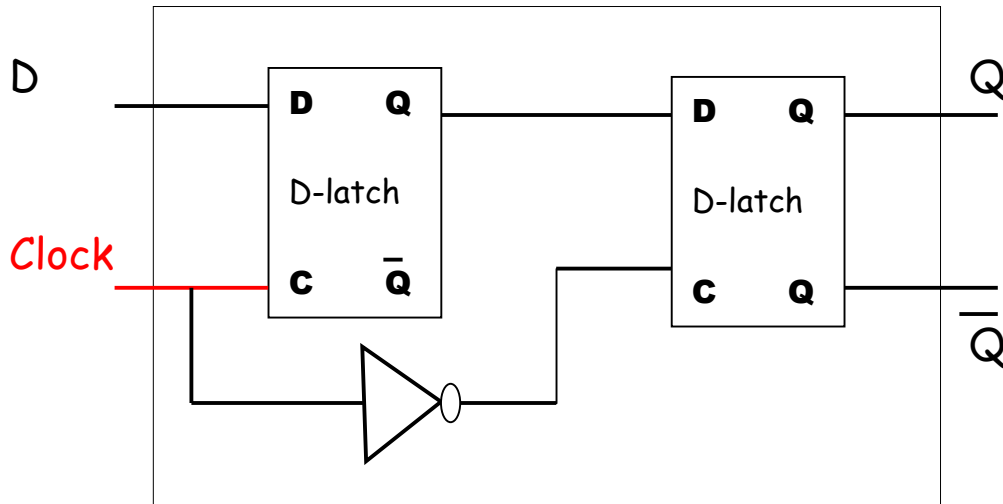
**Clock is the enabler.** If  $C=0$ , Q remains unchanged.

When  $C=1$ , then Q acquires the value of D. We will use it as a building block of sequential circuits.

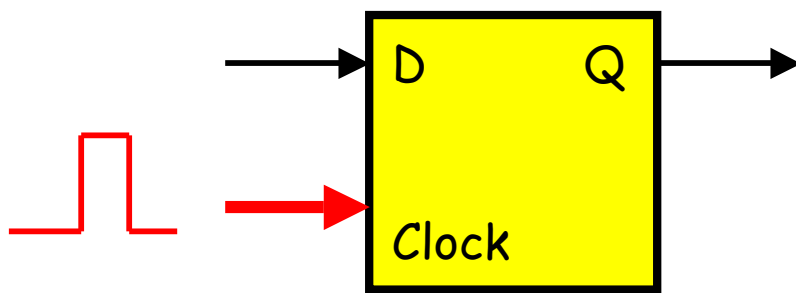


There are some shortcomings of this simple circuit. An **edge-triggered** circuit (or a **master-slave** circuit) solves this problem

# Master-Slave D flip-flop



Internal details shown above



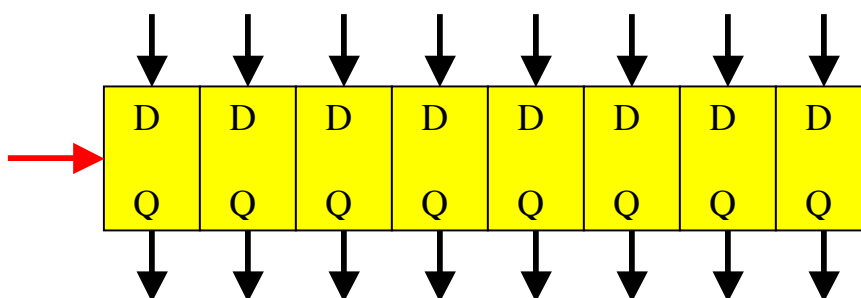
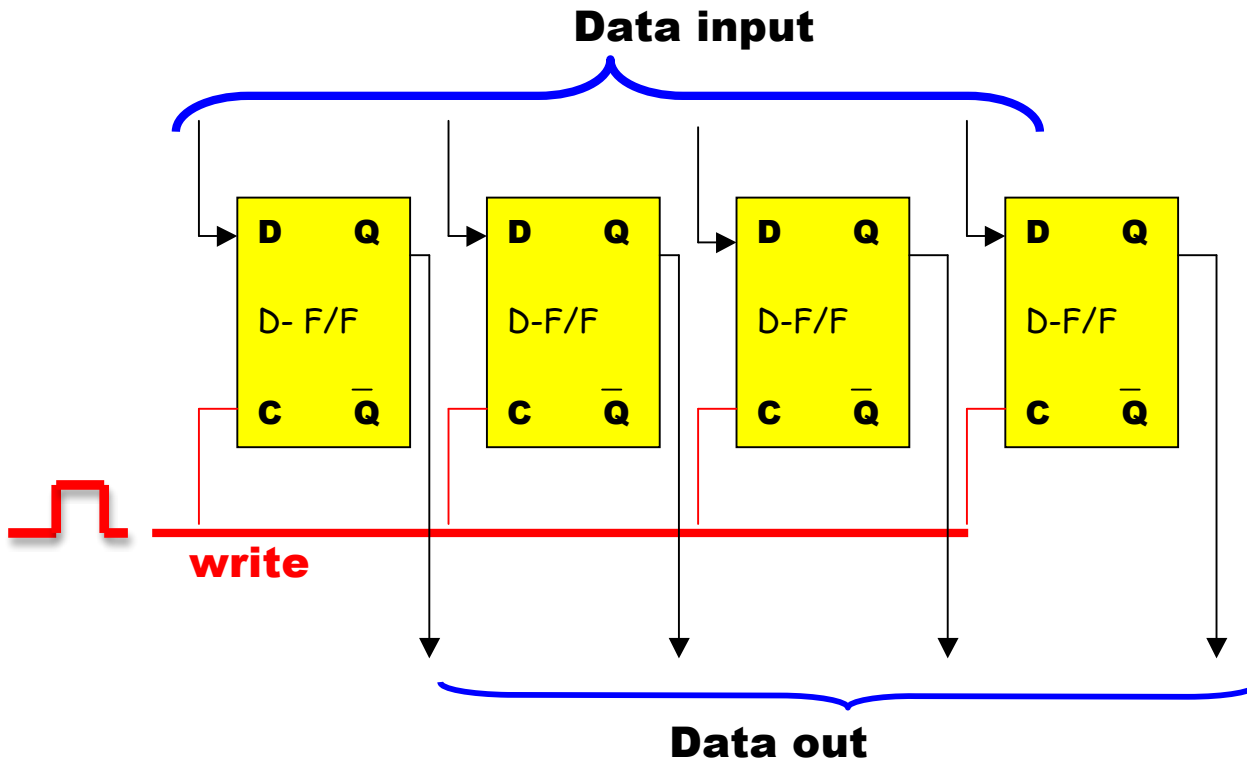
Clock pulse

Abstract view

The output Q acquires the value of the input D, only when **one complete clock pulse** is applied to the clock input.

## Register

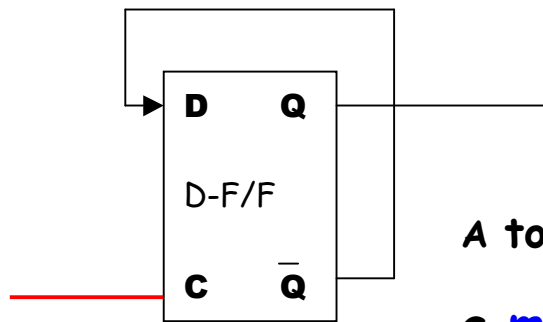
A 8-bit register is an array of 8 D-flip-flops.



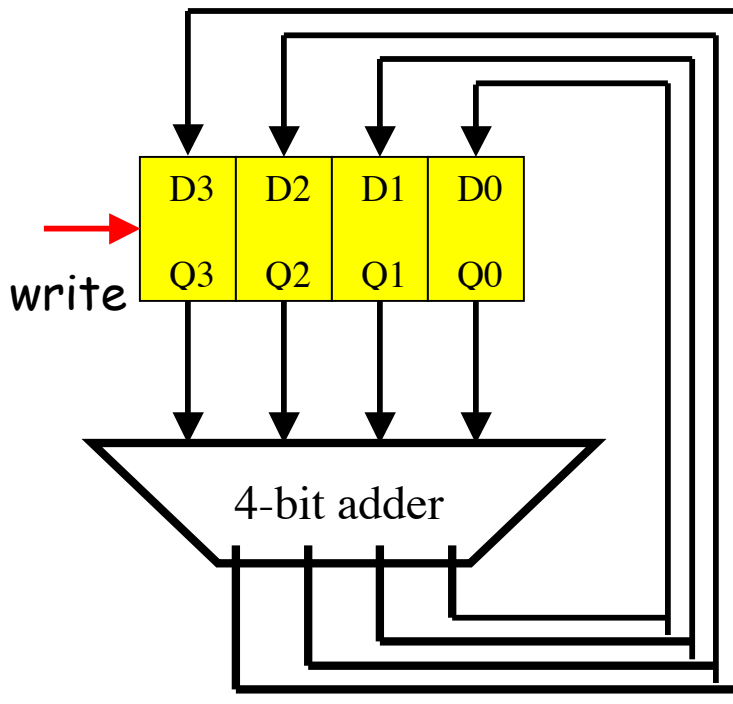
Abstract view of a register

## Binary counter

Counts 0, 1, 2, 3, ...



A toggle flip-flop (T) is  
a **modulo-2 counter**

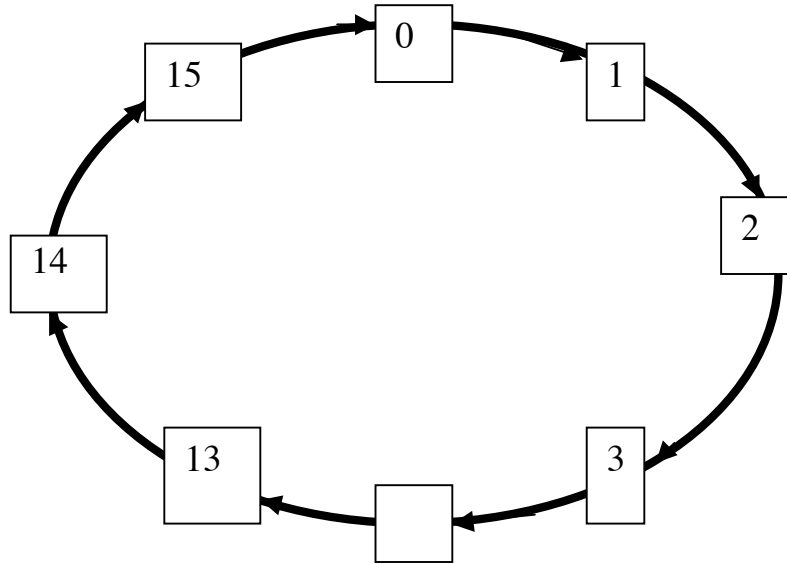


**A 4-bit counter**  
(mod-16 counter)

Observe how Q3 Q2 Q1 Q0 change when pulses are applied to the clock input

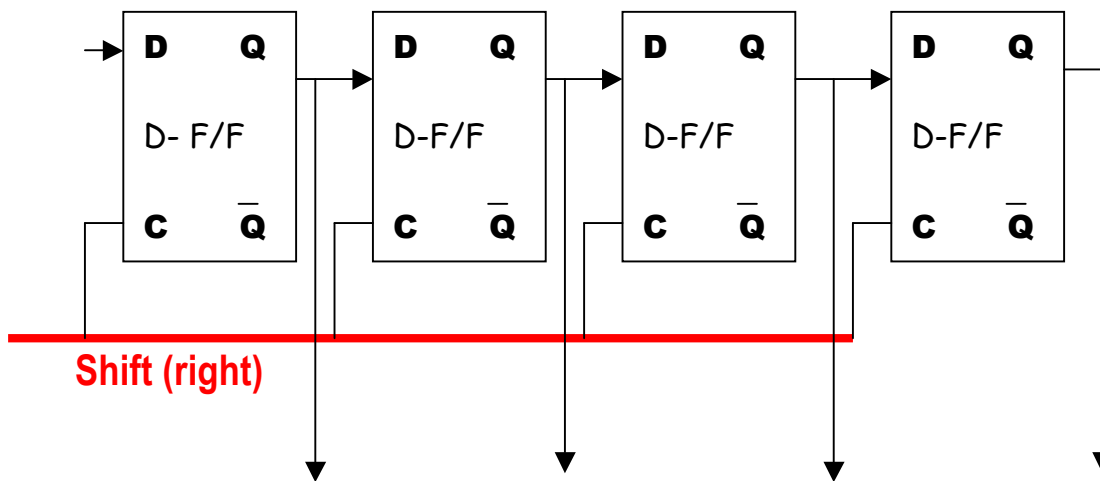
## State diagram of a 4-bit counter

Here state =  $Q_3Q_2Q_1Q_0$



Recall that the program counter is a 32-bit counter

## A shift register



With each pulse

# Hardware Multiplication

Multiplicand				1	0	0	1
Multiplier				1	0	1	0
				0	0	0	0
			1	0	0	1	0
		0	0	0	0	0	0
	1	0	0	1	0	0	0
<b>Product</b>	1	0	1	1	0	1	0

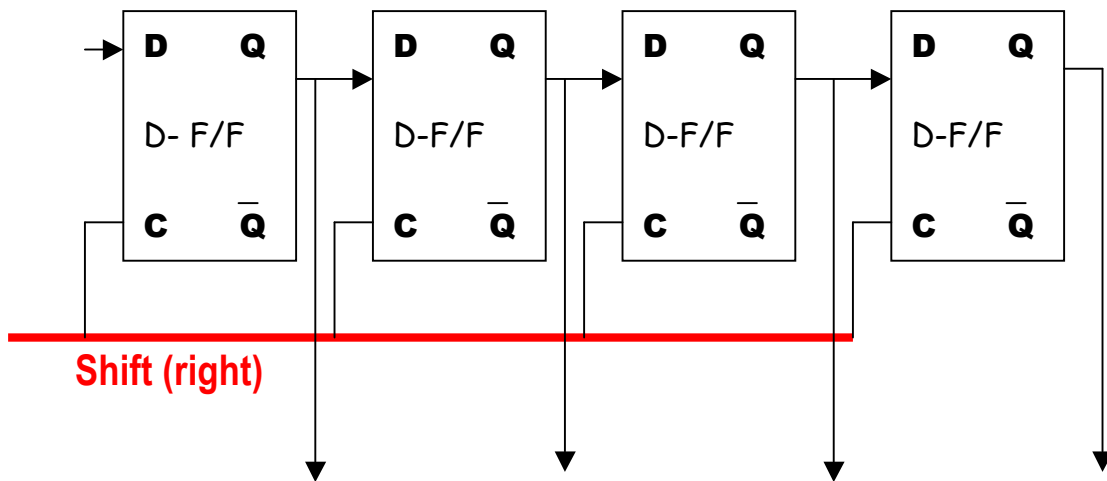
The basic operations are **ADD** and **SHIFT**. Now let us see how it is implemented by hardware.

By now, you know all the **building blocks**.

# The Building Blocks

## A shift register

Review how a D flip-flop works

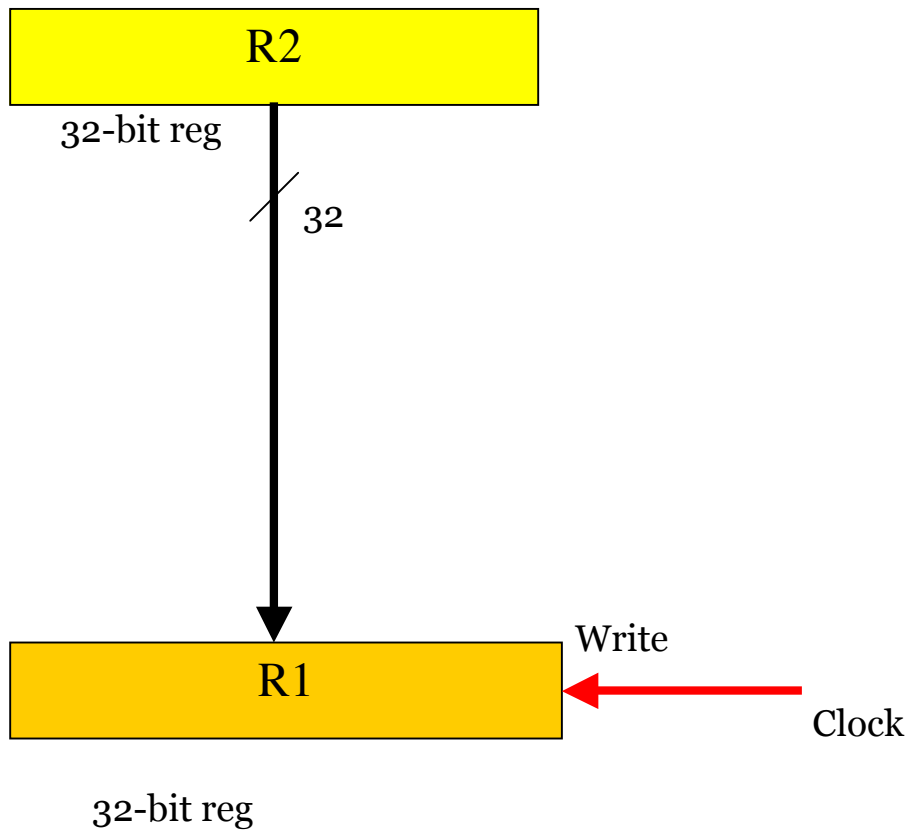


With **each clock pulse** on the shift line, data moves one place to the right.



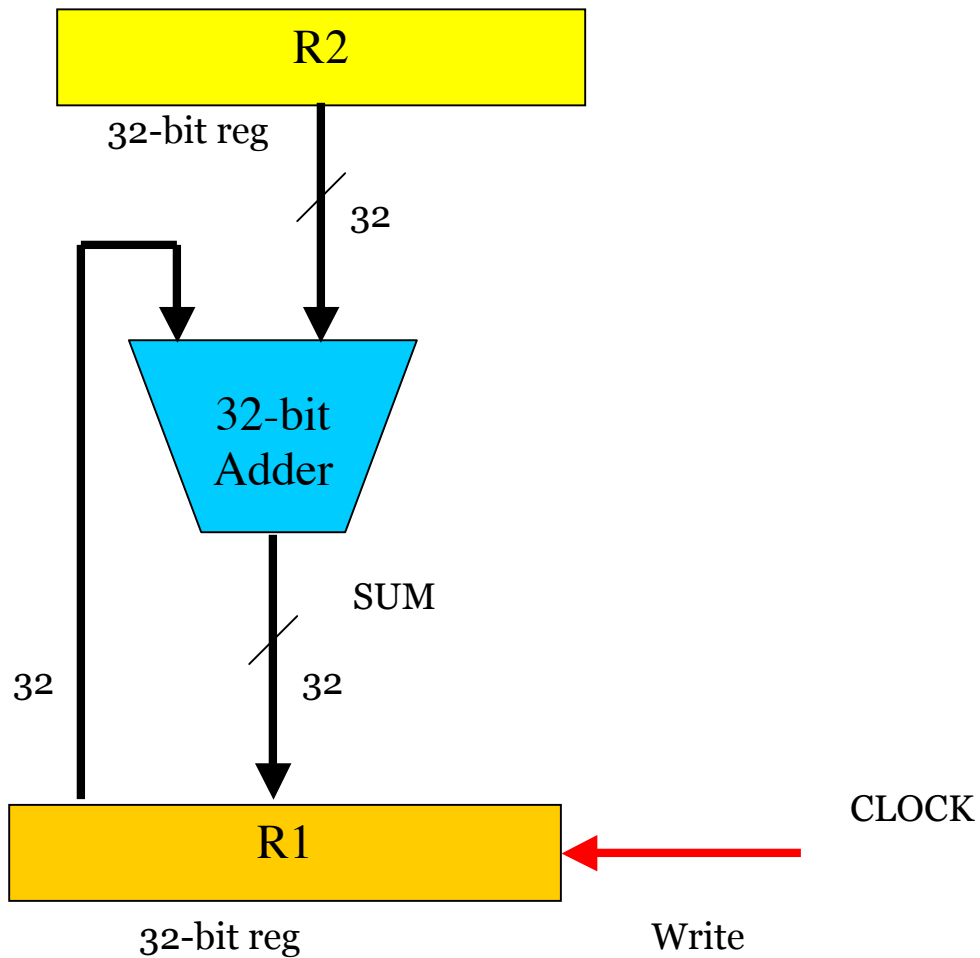
# Executing $r1 := r2$

How to implement a simple register transfer  $r1 := r2$ ?



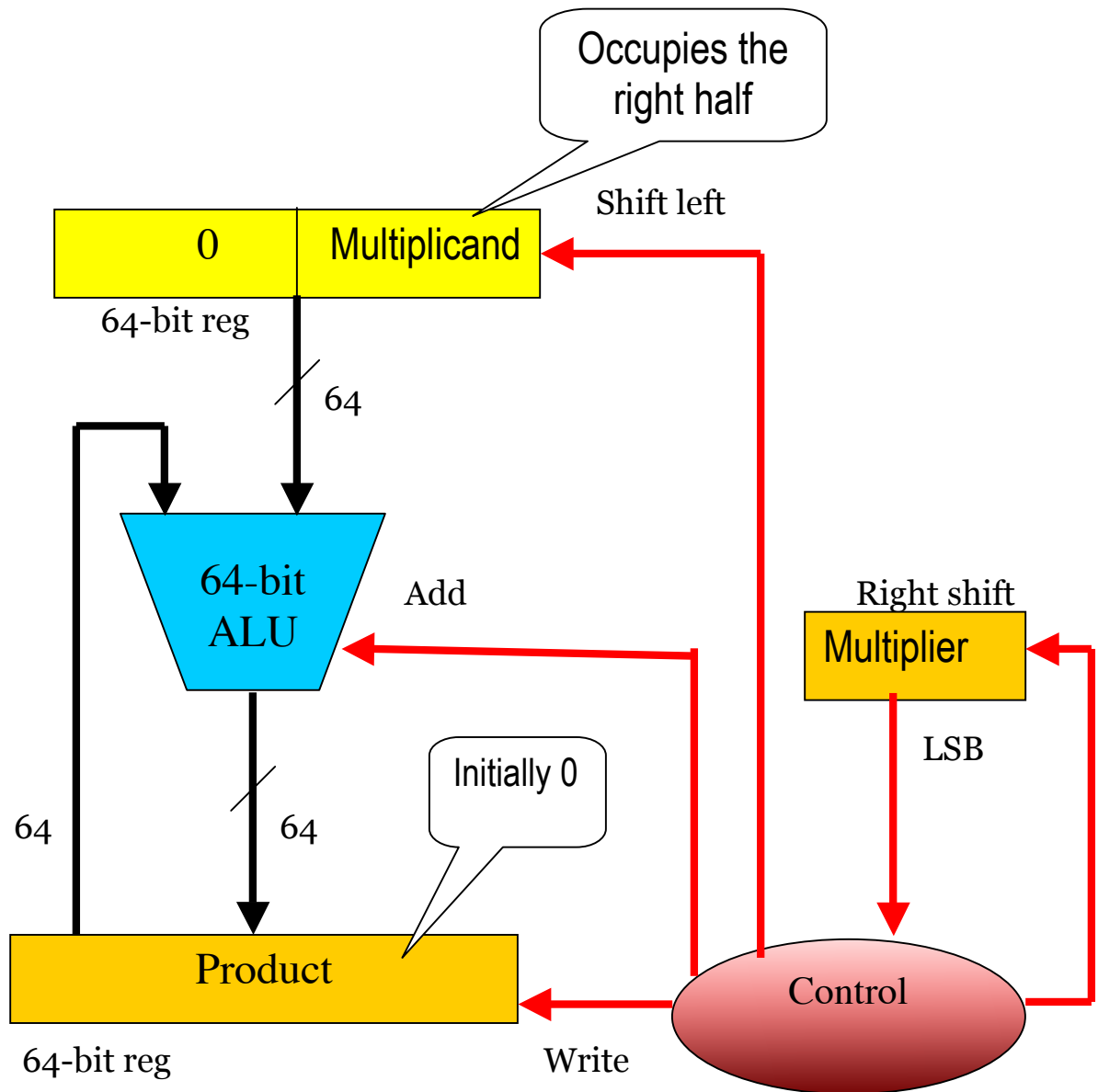
It requires only **one clock pulse** to complete the operation.

# Executing $r1 := r1 + r2$



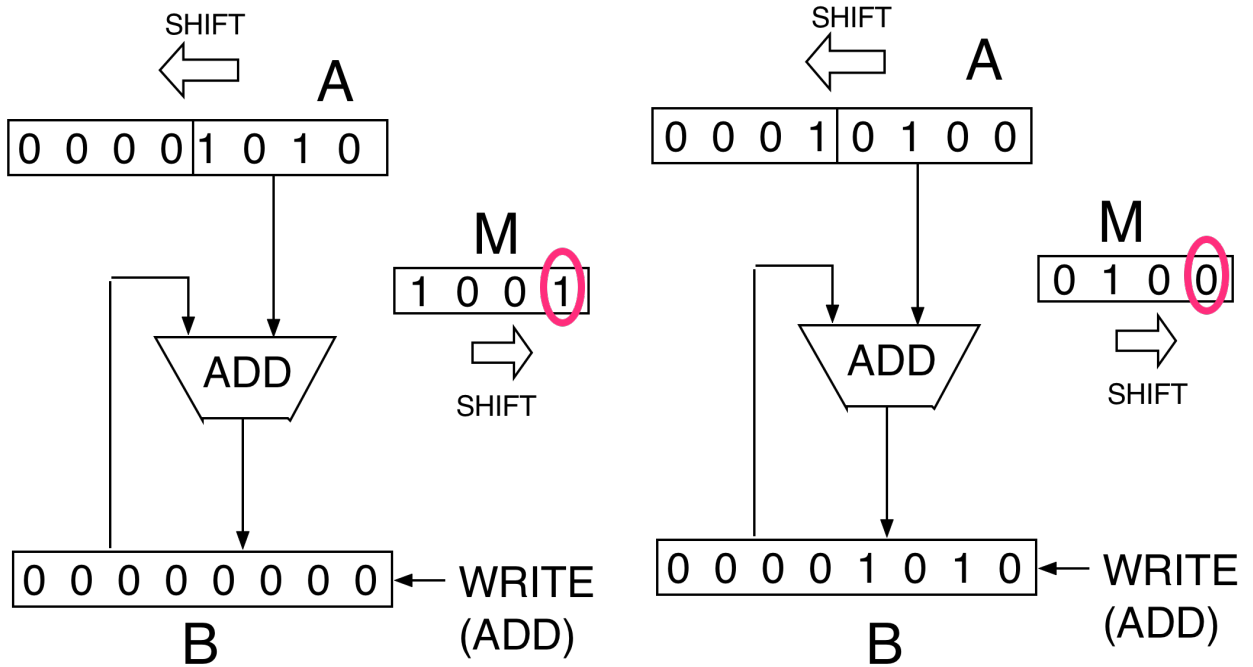
It requires only **one clock pulse** to complete the operation.

# A Hardware Multiplier



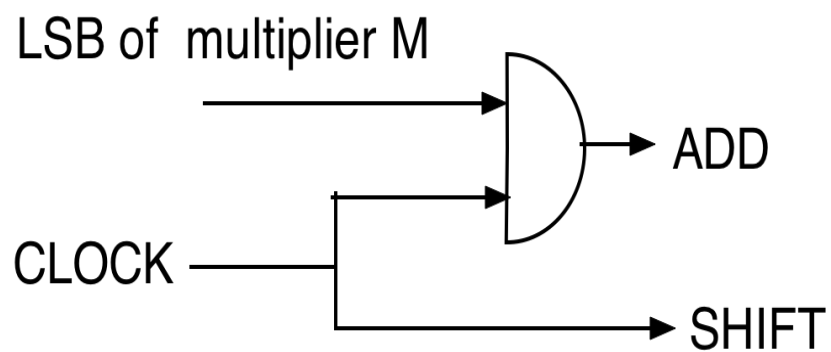
**If LSB of Multiplier = 1 then add else skip;**  
**Shift left multiplicand & shift right multiplier**

How to implement the control unit?



if  $LSB(M) = 1$  then **ADD**, **SHIFT LEFT A**, **SHIFT RIGHT M**

else **SHIFT LEFT A**, **SHIFT RIGHT M**



# Division

The restoring division algorithm follows the simple idea from the elementary school days. It involves subtraction and shift. Here is an implementation by hardware

