

Random Walks and Defining Functions



FEB 16TH

If we take a random walk, will we go places?



- **Problem:** Simulate a *random walk* in which a person starts at point 0 and at each step randomly picks a direction (left or right) and moves 1 step in that direction.
- Take a positive integer n and terminate the simulation when the walk reaches n or $-n$.
- Report the *average* number of steps it took for the walk to terminate.
- Do this for various n and plot the results to get a sense of how rapidly the walk terminates, as a function of n .

The random module



- Programs for games and simulation use *randomization* extensively.
- In games, you want to add an element of randomness to the obstacles or adversaries.
- In simulations (e.g., traffic simulation) you want to introduce actors into your simulation according to certain probability distribution.

Some functions in the `random` module



- `random.randint(a, b)`: return a random integer N such that $a \leq N \leq b$.
- `random.random()`: Return the next random floating point number in the range $[0.0, 1.0)$.
- `random.uniform(a, b)`: Return a random floating point number N such that $a \leq N \leq b$ for $a \leq b$ and $b \leq N \leq a$ for $b < a$.

Simple Example



Problem: Write a program that takes as input a positive integer n and simulates n rolls of two six-sided dice. The program should report the number of times 7 appears as the sum of the outcomes of the two dice rolls.

Solution



```
# Programmer: Sriram Pemmaraju
# Feb 13th, 2013
# This program simulates the roll of two six-sided dice
# as many times as specified by the input. Then the program
# outputs the number of times 7 shows up as the sum of the two
# dice rolls

import random
n = int(raw_input("Enter the number of times you want the dice rolled: "))

counter = 0 # keeps track of the number of rolls
numSevens = 0 # keeps track of the number of sevens

while counter < n:
    sumRolls = random.randint(1, 6) + random.randint(1, 6)
    if sumRolls == 7:
        numSevens = numSevens + 1

    counter = counter + 1

print "The number of sevens is", numSevens
```

Taking a single random step



```
import random
```

```
# Version 1. This program starts off a person at 0 and moves  
# her one step to the left or right, at random.
```

```
location = 0
```

```
step = random.randint(0, 1) # returns 0 or 1, each with prob. 1/2
```

```
if step == 0:
```

```
    step = -1
```

```
location = location + step
```

```
print location
```

Simulating the random walk



```
import random
```

```
# Version 2. This program starts off a person at 0 and moves  
# her left or right, at random one step at a time until she reaches  
# the "barrier" at n or - n.
```

```
n = input("Enter a positive integer: ")  
location = 0
```

```
# Loop terminates when the location reaches n or -n  
while abs(location) != n:  
    step = random.randint(0, 1) # returns 0 or 1, each with prob. 1/2  
    if step == 0:  
        step = -1  
    location = location + step
```

```
print location
```

Counting the length of the random walk



```
import random
```

```
# Version 3. This program starts off a person at 0 and moves  
# her left or right, at random one step at a time until she reaches  
# the "barrier" at n or -n. It outputs the length of the walk.
```

```
n = input("Enter a positive integer: ")
```

```
location = 0 # tracks the location of the person
```

```
length = 0 # tracks the length of the random walk
```

```
# Loop terminates when the location reaches n or -n
```

```
while abs(location) != n:
```

```
    step = random.randint(0, 1) #returns 0 or 1, each with prob. 1/2
```

```
    if step == 0:
```

```
        step = -1
```

```
    location = location + step
```

```
    length = length + 1
```

```
print length
```

What more is there to do?



There are two more things we need to do to solve our problem:

1. Find the average length of a walk, for a particular value n of the barrier. We have to decide how many runs to take the average over.
2. Repeat this for various values of n and try to understand the trend.

We need a loop around our current code to do (1) and another loop around that code to do (2).

Defining a function



- Things have become complicated enough that we need to reorganize our code using functions.
- The plan is to define a function called `randomWalk` that takes n (the barrier distance) as an *argument* and *returns* the length of a simulated random walk.
- We can then just *call* this function from the main part of the program.

The function randomWalk



```
# This function takes the barrier distance n as an argument, simulates  
# the random walk until it hits the barrier (n or -n), and returns the  
# length of the random walk
```

```
def randomWalk( n ):
```

```
    location = 0 # tracks the location of the person
```

```
    length = 0 # tracks the length of the random walk
```

```
# Loop terminates when the location reaches n or -n
```

```
while abs(location) != n:
```

```
    step = random.randint(0, 1) #returns 0 or 1, each with prob. 1/2
```

```
    if step == 0:
```

```
        step = -1
```

```
    location = location + step
```

```
    length = length + 1
```

```
return length
```

Notes about this function



- The first line of the function:



- The body of the function is indented.
- It is as though `n` is input to the function.
- A function can have one or more arguments
- The last line of the function is usually a return:
`return length`

The rest of the program



```
n = input("Enter a positive integer: ")  
print randomWalk(n)
```

- `randomWalk(n)` is a call to the function `randomWalk` providing it the number `n` that the user as input as an argument.
- In order to execute the print statement, the function call `randomWalk(n)` needs to be executed first.
- This means that “control” is transferred to the function and we start executing the function starting with its first line.
- The value that the function returns essentially replaces the function call.

Averaging over 100 simulations



```
n = input("Enter a positive integer: ")
```

```
count = 0 # tracks the number of times the walk is repeated
```

```
sum = 0 # sum of the lengths of the walk; needed for average
```

```
while count < 100:
```

```
    sum = sum + randomWalk(n)
```

```
    count = count + 1
```

```
print float(sum)/100
```

Making another function



```
# This function repeats a random walk with barrier n as many times  
# as specified by the argument numRepetitions and returns the length  
# of the walk, averaged over all the repetitions
```

```
def manyRandomWalks(n, numRepetitions):
```

```
    count = 0 # tracks the number of times the walk is repeated
```

```
    sum = 0 # sum of the lengths of the walk; needed for average
```

```
    # Repeats the random walk as many times as specified by numRepetitions
```

```
    while count < numRepetitions:
```

```
        sum = sum + randomWalk(n)
```

```
        count = count + 1
```

```
    return float(sum)/100
```

The rest of the program



```
n = input("Enter a positive integer: ")  
print manyRandomWalks(n, 100)
```

- The function call needs to supply arguments in the correct order, i.e., in the order specified in the function definition.
- Names in the function call have nothing to do with names in the function definition. We could have written

```
m = input("Enter a positive integer: ")  
print manyRandomWalks(m, 100)
```

And the value of `m` and the value `100` would be used for `n` and `numRepetitions` in the function.

Trying this out for different barrier values



```
m = 10 # tracks the value of the barrier
# m travels through 10, 20, ..., 100 in this loop and we compute and print the
# average walk length for each m
while m <= 100:
    print manyRandomWalks(m, 100)
    m = m + 10
```

Sample output



112.86
376.4
827.6
1628.04
2570.6
3594.2
4616.14
6035.6
8596.58
10948.58

Length of random walk

