

# Random Walks and Defining Functions



**FEB 16TH**

# If we take a random walk, will we go places?



- **Problem:** Simulate a *random walk* in which a person starts at point 0 and at each step randomly picks a direction (left or right) and moves 1 step in that direction.
- Take a positive integer  $n$  and terminate the simulation when the walk reaches  $n$  or  $-n$ .
- Report the average number of steps it took for the walk to terminate.
- Do this for various  $n$  and plot the results to get a sense of how rapidly the walk terminates, as a function of  $n$ .

# Taking a single random step



```
import random
```

```
# Version 1. This program starts off a person at 0 and moves  
# her one step to the left or right, at random.
```

```
location = 0
```

```
step = random.randint(0, 1) # returns 0 or 1, each with prob. 1/2
```

```
if step == 0:
```

```
    step = -1
```

```
location = location + step
```

```
print location
```

# Simulating the random walk



```
import random
```

```
# Version 2. This program starts off a person at 0 and moves  
# her left or right, at random one step at a time until she reaches  
# the "barrier" at n or - n.
```

```
n = input("Enter a positive integer: ")  
location = 0
```

```
# Loop terminates when the location reaches n or -n
```

```
while abs(location) != n:
```

```
    step = random.randint(0, 1) # returns 0 or 1, each with prob. 1/2
```

```
    if step == 0:
```

```
        step = -1
```

```
    location = location + step
```

```
print location
```

# Counting the length of the random walk



```
import random
```

```
# Version 3. This program starts off a person at 0 and moves  
# her left or right, at random one step at a time until she reaches  
# the "barrier" at n or -n. It outputs the length of the walk.
```

```
n = input("Enter a positive integer: ")
```

```
location = 0 # tracks the location of the person
```

```
length = 0 # tracks the length of the random walk
```

```
# Loop terminates when the location reaches n or -n
```

```
while abs(location) != n:
```

```
    step = random.randint(0, 1) #returns 0 or 1, each with prob. 1/2
```

```
    if step == 0:
```

```
        step = -1
```

```
    location = location + step
```

```
    length = length + 1
```

```
print length
```

# What more is there to do?



There are two more things we need to do to solve our problem:

1. Find the average length of a walk, for a particular value  $n$  of the barrier. We have to decide how many runs to take the average over.
2. Repeat this for various values of  $n$  and try to understand the trend.

We need a loop around our current code to do (1) and another loop around that code to do (2).

# Defining a function



- Things have become complicated enough that we need to reorganize our code using functions.
- The plan is to define a function called `randomWalk` that takes  $n$  (the barrier distance) as an *argument* and *returns* the length of a simulated random walk.
- We can then just *call* this function from the main part of the program.

# The function randomWalk



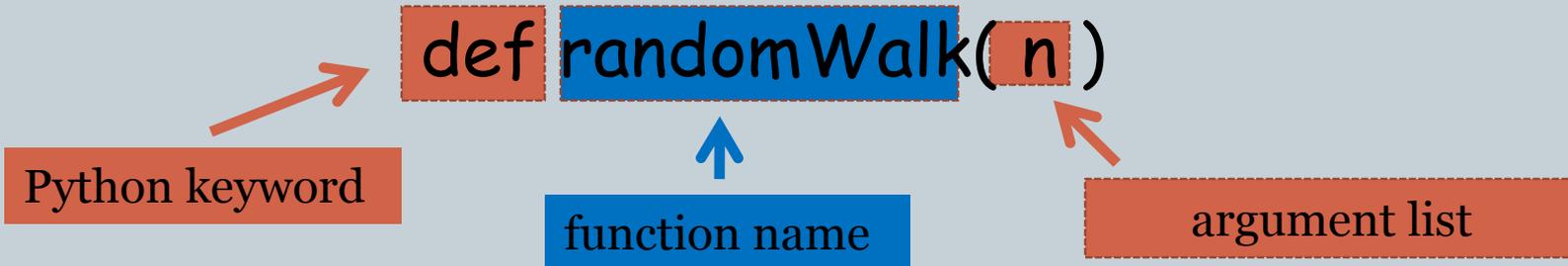
```
# This function takes the barrier distance n as an argument, simulates  
# the random walk until it hits the barrier (n or -n), and returns the  
# length of the random walk
```

```
def randomWalk( n ):  
    location = 0 # tracks the location of the person  
    length = 0 # tracks the length of the random walk  
  
    # Loop terminates when the location reaches n or -n  
    while abs(location) != n:  
        step = random.randint(0, 1) #returns 0 or 1, each with prob. 1/2  
        if step == 0:  
            step = -1  
        location = location + step  
        length = length + 1  
  
    return length
```

# Notes about this function



- The first line of the function:



- The body of the function is indented.
- It is as though `n` is input to the function.
- A function can have one or more arguments
- The last line of the function is usually a return:  
`return length`

# The rest of the program



```
n = input("Enter a positive integer: ")  
print randomWalk(n)
```

- `randomWalk(n)` is a call to the function `randomWalk` providing it the number `n` that the user as input as an argument.
- In order to execute the print statement, the function call `randomWalk(n)` needs to be executed first.
- This means that “control” is transferred to the function and we start executing the function starting with its first line.
- The value that the function returns essentially replaces the function call.

# Averaging over 100 simulations



```
n = input("Enter a positive integer: ")
```

```
count = 0 # tracks the number of times the walk is repeated
```

```
sum = 0 # sum of the lengths of the walk; needed for average
```

```
while count < 100:
```

```
    sum = sum + randomWalk(n)
```

```
    count = count + 1
```

```
print float(sum)/100
```

# Making another function



```
# This function repeats a random walk with barrier n as many times  
# as specified by the argument numRepetitions and returns the length  
# of the walk, averaged over all the repetitions
```

```
def manyRandomWalks(n, numRepetitions):
```

```
    count = 0 # tracks the number of times the walk is repeated
```

```
    sum = 0 # sum of the lengths of the walk; needed for average
```

```
    # Repeats the random walk as many times as specified by numRepetitions
```

```
    while count < numRepetitions:
```

```
        sum = sum + randomWalk(n)
```

```
        count = count + 1
```

```
    return float(sum)/100
```

# The rest of the program



```
n = input("Enter a positive integer: ")  
print manyRandomWalks(n, 100)
```

- The function call needs to supply arguments in the correct order, i.e., in the order specified in the function definition.
- Names in the function call have nothing to do with names in the function definition. We could have written

```
m = input("Enter a positive integer: ")  
print manyRandomWalks(m, 100)
```

And the value of `m` and the value `100` would be used for `n` and `numRepetitions` in the function.

# Trying this out for different barrier values



```
m = 10 # tracks the value of the barrier
# m travels through 10, 20, ..., 100 in this loop and we compute and print the
# average walk length for each m
while m <= 100:
    print manyRandomWalks(m, 100)
    m = m + 10
```

# Sample output



112.86  
376.4  
827.6  
1628.04  
2570.6  
3594.2  
4616.14  
6035.6  
8596.58  
10948.58

**Length of random walk**

