Algorithmic Excursions (CS:4980:0001 or 22C:196:001) Homework 2

The homework is due in class on Thursday, March 24th. If you can't make it to class, drop it in my mailbox in the MacLean Hall mailroom.

- 1. As stated on page 2 of lecture notes for Week 4, show that for any $1 \leq k \leq n$, the set $\{C_1, C_2, \ldots, C_k\}$ of centers computed by the greedy permutation algorithm is a γ_k -packing.
- 2. As stated on page 3 of lecture notes for Week 4, construct an example where the local search algorithm for k-median fails to output an optimal solution.
- 3. As stated on page 6 of lecture notes for Week 5, describe an example where Lloyd's method (also known as the k-means heuristic) terminates with a solution that does not minimize the k-means objective.
- 4. Explore if there are examples where Lloyd's method fails to find the "right clustering", which is a subjective notion. Report on your explorations. How helpful do you think it would be to run the method several times, varying the initial set of centers?