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Let  $S$  be a positive self-adjoint invertible operator on an  $N$ -dimensional Hilbert space  $H_N$  and let  $M \geq N$ . We give necessary and sufficient conditions on real sequences  $a_1 \geq a_2 \geq \dots \geq a_M \geq 0$  so that there is a frame  $\{\varphi_n\}_{n=1}^{n=M}$  for  $H_N$  with frame operator  $S$  and  $\|\varphi_n\| = a_n$ , for all  $n = 1, 2, \dots, M$ . As a consequence, given any *frame operator*  $S$  as above, there is a set of equal norm vectors in  $H_N$  which have precisely  $S$  as their frame operator. A MATLAB toolbox implementing all results is freely distributed by the authors. (Received September 10, 2002)