## Homework VII

## 1. [15 points]

Show that a longest simple path in a (free) tree starts and ends at a leaf node.

## 2. [20 points]

Let $G=(V, E)$ be a (simple) graph and define the following relation on $V$ : $\left(v_{1}, v_{2}\right) \square R$ if there is a simple path of even length (including length 0 ) between $v_{1}$ and $v_{2}$.
(a) Determine the pairs of this relation for the graph below; is it an equivalence relation?

(b) Show that for any (free) tree, this relation is an equivalence relation on the vertices.

## 3. [20 points]

Problem 1, page 407 of our text.

## 4. [20 points]

Trace Dijkstra's algorithm for finding a shortest path from node a to node d in the digraph below.


