

## Homework I

### 1. [10 points]

Show that for any wffs  $\phi$ ,  $\psi$  and  $\chi$  the propositional formula  $((\phi \rightarrow \psi) \rightarrow (\phi \rightarrow \chi)) \rightarrow (\psi \rightarrow \chi)$  is a tautology.

### 2. [15 points]

Provide an expression utilizing *only* the '**nand**' operation (negated 'and', see truth table definition below) that is logically equivalent to each of the three usual Boolean operations  $\neg$ ,  $\wedge$ , and  $\vee$ .

| P | Q | P <b>nand</b> Q |
|---|---|-----------------|
| T | T | F               |
| T | F | T               |
| F | T | T               |
| F | F | T               |

### 3. [10 points]

Show that  $(x \text{ **nand** } y) \text{ **nand** } z$  is not logically equivalent to  $x \text{ **nand** } (y \text{ **nand** } z)$  (i.e., **nand** is not associative).

### 4. [10 points]

Determine if the program assertion (see Chapter 14 of Diller) below is valid and justify your answer. Assume that the domain of the program variables is integers.

```

      {true}
  if X>Y then skip else X:= X*X*Y
      {X>Y}

```