

Errata in *Programming Language Foundations*

Aaron Stump
Computer Science
The University of Iowa

October 11, 2016

Corrections below

Despite many previous readings, attentive readers have found some errors in the book. I correct these below, sometimes underlining changes to the text. Thanks to the following people for reporting bugs: Ryan Brummet, Junyang Chen, Wyatt Kaiser, Tingting Liu, Talal Riaz, John Bodeen.

Chapter 1

1. page 28, second to last case of the proof. The sentence should say “So by the induction hypothesis, we have that $\llbracket t_1 \rrbracket \sigma'$ and $\llbracket t_2 \rrbracket \sigma'$ are both defined and equal to $\llbracket t_1 \rrbracket \sigma$ and $\llbracket t_2 \rrbracket \sigma$, respectively.”
2. page 30, Section 1.14.2, problem 2. The theorem cannot be proved without some additional assumption. So the revised problem is:

2. Let us temporarily define $\sigma \leq \sigma'$ for assignments σ and σ' to mean that for all variables x , if $\sigma(x)$ is defined then so is $\sigma'(x)$ and we have $\sigma(x) \leq \sigma'(x)$. Suppose that t is a term which does not contain the negation or subtraction symbols, and suppose that σ is an assignment where $0 \leq \sigma(x)$ for every variable x . Prove by induction on the structure of t that if $\sigma \leq \sigma'$, then $0 \leq \llbracket t \rrbracket \sigma \leq \llbracket t \rrbracket \sigma'$. (You can use the proof of Theorem 1.11.1 as a guide.)

Chapter 2

1. page 35, top of the page: it says we can “easily define the syntax for all commands except **while**-commands”, but it should say “easily define the semantics for all commands except **while**-commands”.
2. page 45, proof of Theorem 2.5.4. In the proof, I wrote “ $f(c(n)) \sqsubset f(\perp c)$ ”. It should say “ $f(c(n)) \sqsubseteq f(\perp c)$ ” instead (we are not using the \sqsubset symbol in this chapter).

Chapter 3

1. page 92, start of Section 3.8. It should say “This means that the strongest formula is *False* and the weakest is *True*.” (The book has *False* and *True* reversed.)

Chapter 4

- page 100. The multi-step derivation at the bottom of the page has a bug in the left branch (a proof rule is not being correctly applied). The correct derivation is:

$$\frac{\frac{\frac{x := 1, \sigma \rightsquigarrow \sigma[x \mapsto 1]}{x := 1; y := 2, \sigma \rightsquigarrow y := 2, \sigma[x \mapsto 1]}}{x := 1; y := 2, \sigma \rightsquigarrow^* y := 2, \sigma[x \mapsto 1]} \quad \frac{\frac{y := 2, \sigma[x \mapsto 1] \rightsquigarrow \sigma[x \mapsto 1, y \mapsto 2]}{y := 2, \sigma[x \mapsto 1] \rightsquigarrow^* \sigma[x \mapsto 1, y \mapsto 2]}}{x := 1; y := 2, \sigma \rightsquigarrow^* \sigma[x \mapsto 1, y \mapsto 2]}}$$

- page 120, part 1 of problem 4.5.1. The final state should be $\{x \mapsto -10, y \mapsto 20, z \mapsto -1\}$, not $\sigma[z \mapsto -1]$.
- page 120, part 1 of problem 4.5.2. The problem should be asking for a reduction sequence (using the small-step operational semantics), not a single small-step derivation. So the problem can be changed to:

Write a sequence of reduction steps (with the small-step semantics) which show how to reduce the following command and starting state to the final state $\{x \mapsto 90\}$. You do not need to give derivations proving your individual small steps.

`if $x < 100$ then $x := x * 10$ else skip, $\{x \mapsto 9\}$`

- page 120, part 2 of problem 4.5.2. The final state should be $\{x \mapsto 14, y \mapsto 3\}$, not $\{x \mapsto 14, y \mapsto 1\}$.
- page 121, part 4 of problem 4.5.2. The problem asks you to find a command c' making a particular small-step judgment is provable, but that judgment mentions c rather than c' . It should mention c' .

Chapter 8

- page 209, Figure 8.2: we are missing the rule for `skip`, which is:

$$\frac{}{\text{skip}, \sigma \rightsquigarrow \sigma}$$

- page 218, example command using `await`: to get correct behavior, the command should await $y+y' = 0$, rather than $y * y' = 0$. Also, we should initialize z and z' to 1 before the concurrently executing commands begin. So change the definition of $exp_{z,y,n}$ to be

$$exp_{z,y,n} = (\text{while } y > 0 \text{ do } y := y - 1; z := z * n)$$

and then use this for the command:

$$y := x; y' := x; z := 1; z' := 1; \\ (\text{exp}_{z,y,2} \parallel \text{exp}_{z',y',3} \parallel \text{await } y + y' = 0 \text{ then } z := z + z')$$

- page 221, Figure 8.8. The third rule in the figure (the one on the right) should have stars on all the arrows:

$$\frac{P \xrightarrow{\gamma}^* P'' \quad P'' \xrightarrow{\gamma'}^* P'}{P \xrightarrow{\gamma\gamma'}^* P'}$$

- page 223. Several arrows – the ones for multi-step reduction – are missing their stars (as in the issue noted just previously).
- page 227, part 3 of problem 8.8.2: there is an `od` missing at the end of the displayed statement.
- page 227, part 1 of problem 8.8.3. The judgment to prove should have \rightsquigarrow^* instead of \rightsquigarrow .